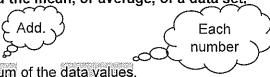
Measures of Center

Success for English Learners

Problem 1

Steps to find the mean, or average, of a data set,

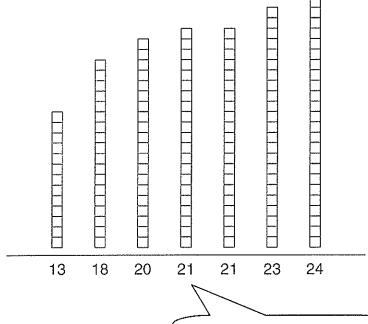


- 1. Find the sum of the data values.
- 2. Divide the sum by the number of data values.

Count each number.

Problem 2

Use a visual model to examine the data.



The mean is the average. sum of data values = number of data values 13+18+20+21+21+23+24

The median is the middle value of an ordered data set.

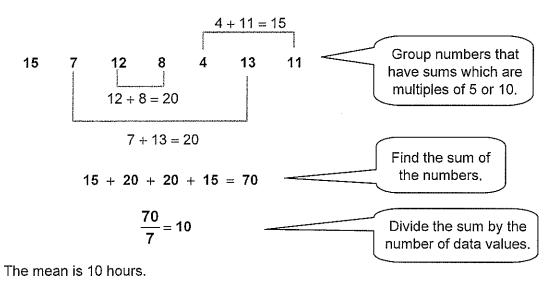
- 1. What is an "ordered data set"?
- 2. How do you find the median if there are an even number of data values?

Measures of Center

Reteach

When calculating the mean, you can use compatible numbers to find the sum of the data values. Compatible numbers make calculations easier. For example, adding multiples of 5 or 10 is easier than adding all of the individual data values.

A group of students are asked how many hours they spend watching television during one week. Their responses are: 15, 7, 12, 8, 4, 13, 11. What is the mean?



Use compatible numbers to find the mean.

1. The costs (in dollars) of items on a lunch menu are 9, 14, 11, 6, 16, 10.

2. The numbers of students in Mr. Silva's math classes are 19, 18, 22, 24, 20, 18, 26.

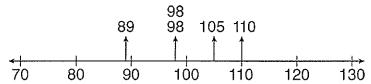
Mean: ____

3. In the television viewing data above, is there more than one way to pair the data values to form compatible numbers? Explain.

Measures of Center

Reading Strategies: Use Graphic Aids

Tim's bowling scores from 5 different games are 89, 98, 110, 98, 105. The scores are shown on the number line below. The number line is a graphic aid that lets you see whether the scores are close together or spread apart.



Use the bowling scores above to complete Exercises 1-3.

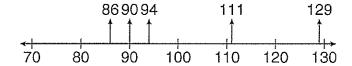
- Are the bowling scores close together or spread out?
- 2. Find the mean and the median bowling scores.

Median:

3. Does one measure describe the data better than the other? Explain.

The number line below shows Pranav's bowling scores from 5 different games. The scores, shown on the number line, are: 94, 90,

111, 86, 129. Use the number line to complete Exercises 4-6.



- 4. Are the bowling scores close together or spread out? _____
- 5. Find the mean and the median bowling scores.

Mean: _____ Median: ____

6. Does one measure describe the data better than the other? Explain.

7. Explain why you think the mean and median are called "measures of center."

Name	Date	Class	



Measures of Center

Practice and Problem Solving: A/B

Use the situation below to complete Exercises 1-4.

The heights	(in inches)	of the starting	ig players	on a high	school l	basketball
team are as	follows: 72	, 75, 78, 72,	73.			

eam	are as follows: 72, 75, 78, 72, 73.		
1. F	low many starting players are there?		
2. V	Vhat is the mean height?		
3. V	Vhat is the median height?		
4. [oes one measure describe the data	better than the other? Explain.	
	ercises 5–7, find the mean and me Daily high temperatures (°F): 45, 50, 4		
Λ	lean:	Median:	
6. E	Brian's math test scores: 86, 90, 93, 8	5, 79, 92	
٨	lean:	Median:	
7. F	Players' heart rates (beats per minute)): 70, 68, 70, 72, 68, 66, 65, 73	
Ν	1ean:	Median:	
n	likers spent the following amounts of ature hike: 48, 46, 52, 57, 58, 52, 61, Find the mean and median times.	• • • • • • • • • • • • • • • • • • • •	
	Mean:	Median:	
t	o. Does one measure describe the d	ata better than the other? Explain.	
Ć		ninutes to complete the hike. Find the this new time.	
	Mean:	Median:	
C	I. Does one measure describe the d	ata better than the other now? Explain.	

	4
Name	

Data	Clace	
Date	Class	

Measures of Center

Practice and Problem Solving: C

Find the mean and median of each data set.

1. Monthly rainfall (in inches): 7.6, 6.7, 8.1, 6.2, 6.0, 6.2

Mean: _____

Median: _____

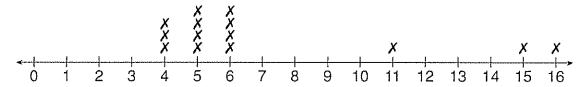
2. Dylan's weekly earnings (in dollars): 200, 167, 185, 212, 195, 193, 188, 140

Mean: _____ Median: ____

3. Fundraising calendars sold per person: 22, 13, 47, 11, 8, 16, 15, 14, 13, 17

Median: _____

The line plot below shows the number of kilometers Clara ran each day for 14 days. Use the line plot for Exercises 4 and 5.



- 4. Find the mean and median for the data.
- 5. Does one measure describe the data better than the other? Explain.

In Exercises 6 and 7, use the given measure to find the missing value in each data set.

6. The mean of the ages of 5 brothers is 13 years.

12, 16, | , 14, 8

7. The median number of students in each music class is 19 people.

16, , 24, 17, 20, 21

8. Write a data set where both the mean and the median describe the data equally well. Explain your reasoning.

Name	Date	Class	



Measures of Center

Practice and Problem Solving: D

Use the situation below to complete Exercises 1 and 2. The first step in Exercise 1 is done for you.

The heights (in meters) of the trees in a park are as follows: 7, 11, 9, 7, 6, 8.

- 1. Follow the steps to find the mean.
 - a. Find the sum of the data values.

48

b. Divide to find the mean.

Mean =
$$\frac{\text{sum of data values}}{\text{number of data values}} = \frac{\square}{\square} = \square$$

The mean height is _____

- 2. Follow the steps to find the median.
 - a. Write the data values in order from least to greatest.
 - b. Find the middle value.

The data set has two middle values: _____ and _____.

Median =
$$\frac{ + }{ } = \frac{ }{ } = \frac{ }{ }$$

The median height is _____.

The points scored by a football team in each game are shown in the table. Use this data to complete Exercises 3–5. The first one is done for you.

3. How many data values are there?

6

4. What is the mean and median?

Mean: _____

Median: _____

Game	Points Scored
1	7
2	20
3	24
4	17
5	28
6	24

5. Does one measure describe the data better than the other? Explain.

least

lower

quartile

70 76 76 80 80 86 87 89 90

median

upper

quartile

greatest

LESSON

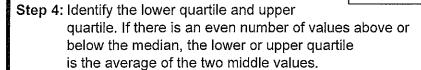
Box Plots

A box plot gives you a visual display of how data are distributed.

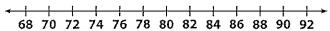
Here are the scores Ed received on 9 guizzes: 76, 80, 89, 90, 70, 86,

87, 76, 80.

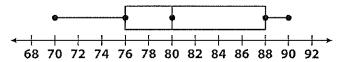
- Step 1: List the scores in order from least to greatest.
- Step 2: Identify the least and greatest values.
- Step 3: Identify the median. If there is an odd number of values, the median is the middle value.



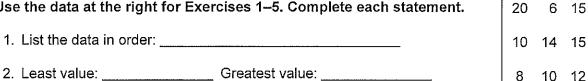




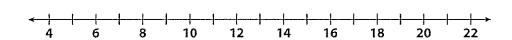
Step 6: Place dots above the number lines at each value you identified in Steps 2-4. Draw a box starting at the lower quartile and ending at the upper quartile. Mark the median, too.



Use the data at the right for Exercises 1-5. Complete each statement.



- 3. Median:
- 4. Lower quartile: Upper quartile:
- 5. Draw a box plot for the data.



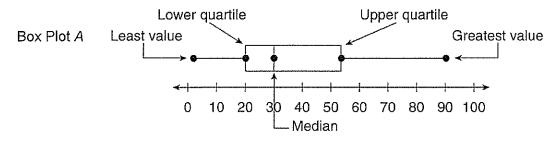


Success for English Learners

A **box plot** shows a set of data divided into four equal parts.

Problem 1

A box plot shows how the values in a data set are distributed or spread out.



Problem 2

To make a box plot, start by putting the data in order from least to greatest.

Identify the least and greatest values. In box plot *A*, the least value is 2 and the greatest value is 90.

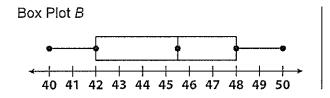
Identify the middle value. This is the **median**. The median for box plot *A* is 30.

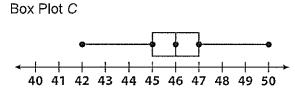
Identify the lower quartile. The **lower quartile** is the middle value between the least value and the median. In box plot *A*, the lower quartile 20.

Identify the upper quartile. The **upper quartile** is the middle value between the median and the greatest value. In box plot *A*, the upper quartile 53.

Plot each identified value on a number line and draw a box from the lower quartile to the upper quartile with a line drawn at the median. Draw a line segment from the least value to the lower quartile and from the upper quartile to the greatest value.

Use box plot B and box plot C to complete the table.





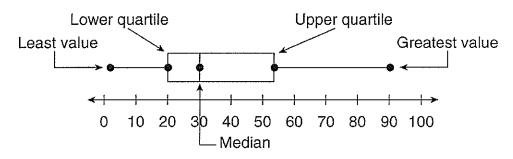
		Median	Least Value	Greatest Value	Lower Quartile	Upper Quartile
1.	Box Plot B					
2.	Box Plot C					

3. Which box plot has the middle half of the data closer together?



Reading Strategies: Use Graphic Aids

A box plot shows a set of data divided into four equal parts called quartiles.



- The median score divides the set of data in half. The median score for this plot is 30.
- The box shows the middle half of the data, located on either side of the median. The box extends from 20 to 53.
- The two "whiskers" identify the remaining half of the data. One whisker extends from the box to the greatest value: from 53 to 90. The other whisker extends from the box to the least value: from 2 to 20.

Answer each question.

- 1. What does the box stand for in a box plot?
- 2. How are the whiskers determined?
- 3. Why is it important to find the median score?

Describe where these scores are located in the box plot above.

- 4. 18 is between the _____ and the _____.
- 5. 75 is between the _____ and the _____.
- 6. 45 is between the _____ and the _____.

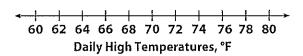
Practice and Problem Solving: A/B

The high temperatures for 2 weeks are shown at the right. Use the data set for Exercises 1–7.

1. Order the data from least to greatest.

High Temperatures
69 73 72 66 64 64 61
70 78 78 74 69 61 62

- 2. Find the median.
- 3. Find the lower quartile. _____
- 4. Find the upper quartile.
- 5. Make a box plot for the data.



- 6. Find the IQR.
- 7. Find the range.

Use the situation and data given below to complete Exercises 8-10.

Two classes collected canned food for the local food bank. Below are the number of cans collected each week.

Class A: 18 20 15 33 30 23 38 34 40 28 18 33

Class B: 18 27 29 20 26 26 29 30 24 28 29 28

8. Arrange the data for each class in order from least to greatest.

Class A:

Class B:

9. Find the median, the range, and the IQR of each data set.

Class A: median:_____ range:____ IQR:____

Class B: median:_____ range:____ IQR:_____

10. Compare and contrast the box plots for the two data sets.

	•		
, Name		Date	

\sim	ass	



Practice and Problem Solving: C

Use the data set at the right for Exercises 1-3.

A math test had 50 questions. The data set shows how many questions were answered correctly in one class.

1. What is the first step you need to do to make a box plot? Complete that step now.

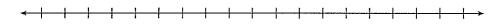
Questions Correctly Answered 48 50 48 40 42 42 47 48 48 41 40 48 43 49 50 43 47 43 42 44

2. Find the median, the range, and the IQR of the data set.

median:

range:_____ IQR:____

3. Make a box plot for the data.



Questions Correctly Answered

Use the situation below to complete Exercises 4–7.

Below are the prices of various rooms at two different resort city hotels.

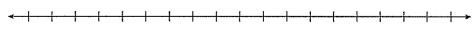
Hotel A: 360 100 180 220 240 200

Hotel B: 300 250 180 80 120 340 220

4. Make box plots for each set of data.

Hotel A





Comparative Room Rates

- 5. Which hotel has the greater median room price?
- 6. Which hotel has the greater interquartile range of room prices?
- 7. Which hotel appears to have more predictable room prices? Explain.

Box Plots

Practice and Problem Solving: D

The data set at the right shows the money Joe earned in 8 weeks. Use the data set to complete Exercises 1–7. The first one is done for you.

Weekly Earnings (\$) 20 12 10 6 12 15 8 15

1. Order the data from least to greatest.

- 2. Find the median.
- 3. Find the lower quartile.
- 4. Find the upper quartile.
- 5. Complete the box plot for the data.



- 6. Find the IQR.
- 7. Find the range.

Use the situation and data given below to complete Exercises 8-11.

Below are the number of books read each week for Juan and Mia.

Juan:

2, 6, 4, 1, 2, 6, 8, 4, 3

Mia:

6, 6, 2, 5, 2, 2, 4, 5, 6

8. Arrange the data for each person in order from least to greatest.

Juan: _____

N // i ~ :

- 9. Who had the higher median number of books read?
- 10. Who had the greater range in number of books read?
- 11. Who had the higher IQR in number of books read?



Reading Strategies: Build Vocabulary

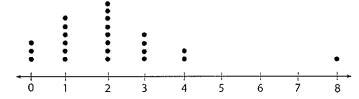
When people study data, they are often asked questions that have a mathematical answer. Some such questions are **statistical**, meaning they have answers that can vary. Some are **not statistical**, meaning they have a single correct answer. For example:

Statistical question: How many books does a typical student read in a week?

Not a statistical question: How many books did Dave read last week?

Statistical questions are answered by collecting and analyzing data.

The data below was collected as an answer to the statistical question above. The data is shown in the dot plot at the right.

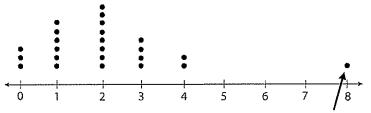


A **dot plot** is a visual way of displaying data.

4	2	1	0	3	2	4	1
1	2	3	8	2	1	0	2
2	3	3	1	1	2	2	0

You can describe the spread, the center, and the shape of a dot plot.

Spread: Range or difference between least and greatest values



The shape of this dot plot is not symmetrical, which means there are more dots on one side of the center of the range than on the other side of center.

An outlier is a data value much greater or less than other data values.

Measures of center:

Mean: Sum of data values
Number of data values

Median: Middle value

data value much Mean, median, and range greater or less might be affected by an **outlier**.

Use the dot plot above to answer each question.

1. How would you describe the spread of the dot plot?

2. What is the mean? What is the median?

3. What do you think it means if a dot plot is symmetrical?

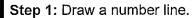
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Dot Plots and Data Distribution

Reteach

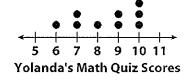
A dot plot gives you a visual display of how data are distributed.

Example: Here are the scores Yolanda received on math quizzes: 6, 10, 9, 9, 10, 8, 7, 7, and 10. Make a dot plot for Yolanda's quiz scores.



Step 2: Write the title below the number line.

Step 3: For each number in the data set, put a dot above that number on the number line.



Yolanda's Math Quiz Scores

Describe the dot plot by identifying the range, the mean, and the median.

Step 4: Identify the range. 10 - 6 = 4

Step 5: Find the mean. $76 \div 9 = 8.4$

Step 6: Find the median. 9

Range: Greatest value - least value

Mean: Sum of data values
Number of data values

Median: Middle value

Use the data set at the right to complete Exercises 1-4.

1. Draw a dot plot for the data.

 Game Scores

 12
 6
 15
 10

 14
 15
 8
 10

 12
 21
 15
 8



- 2. Find the range.
- 3. Find the mean.
- 4. Find the median.



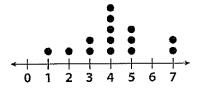
Success for English Learners

A dot plot provides a visual way to display data.

Problem 1

The data below is shown in the dot plot at the right.

Summer Hours I Spent Horseback Rídíng

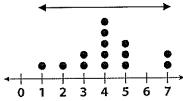


Summer Hours I Spent Horseback Riding

Problem 2

You can describe the spread, the center, and the shape of a dot plot.

Spread: Range or difference between least and greatest values



The **shape** of this dot plot is **symmetrical**, which means there are about the same number of dots on one side of the center of the range as on the other side of center.

How would you describe the spread of the dot plot?

Measures of center:

Mean: Sum of data values

Number of data values

Median: Middle value

- 2. Find the mean of the data.
- 3. Find the median of the data.
- 4. What does it mean if the shape of a dot plot is not symmetrical?

Practice and Problem Solving: A/B

Tell whether each question is a statistical question. If it is a statistical question, identify the units for the answer.

- 1. How far do you travel to get to school?
- How tall is the door to this classroom?

Use the data set at the right and the description below to complete Exercises 3-6.

The class took a survey about how many people live in each student's home. The results are shown at the right.

3. Make a dot plot of the data.

People in Our Homes 4, 2, 5, 4, 2, 6, 4, 3, 4, 3, 5, 6, 2, 7, 3, 2, 5, 3, 4,11, 4, 5, 3



4. Find the mean, median, and range of the data.

mean: ; median: ; range: _____;

5. Describe the spread, center, and shape of the data distribution.

6. Which number is an outlier in the data set? Explain what effect the outlier has on the measures of center and spread.

7. Survey 12 students to find how many people live in their homes. Record the data below. Make a box plot at the right.

i e		
Vame	Date	Class
vanie	Date	Class



Practice and Problem Solving: C

Use the data set at the right and the description below to complete Exercises 1–4.

The class counted the cars in the parking lot each hour from 9 $\,\mathrm{A.M.}$ to 4 $\,\mathrm{P.M.}$ for 3 days. The results are shown in the data set.

1. Make a dot plot of the data.

Cars in the Parking Lot 30, 22, 33, 22, 26, 24, 33, 8, 30, 33, 40, 28, 38, 30, 38, 33, 33, 28, 22, 28, 30

		,		1		- 1	1	ſ	1	- 1	1	ı	- 1	1	1	1.
4				-1-						.		1			T	
8	10	12	14	16	18	20	22	24	26	28	30	32	34	36	38	40
	Cars in the Parking Lot															

	Cars in the Parking Lot
2.	Find the mean, median, and range of the data.
	mean:; median:; range:
3.	Describe the spread, center, and shape of the data distribution.
4.	Which number is an outlier in the data set? Explain what effect the outlier has on the measures of center and spread.
Δns	swer the questions below.
	Write a survey question that you can ask at least 15 people.
6.	Complete your survey. List the results.
7.	In the blank space at the right, make a dot plot to show the results of your survey.
8.	Find each of the following.
	mean:; median:; range:

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Practice and Problem Solving: D

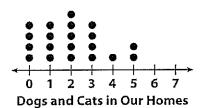
Use the data set at the right and the description below for Exercises 1-3. The first one is done for you.

The class took a survey about how many dogs and cats each student has. The results are shown in the data set.

1. Make a dot plot of the data.

Dogs and Cats in Our Homes

1, 0, 3, 5, 1, 3, 2, 4, 2, 1, 2, 0, 5, 3, 1, 2, 0, 0, 2, 3



2. Find the mean, median, and range of the data.

mean: ; median: ; range:_____

Choose the best description of shape of the data distribution.

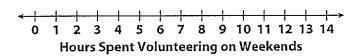
A. symmetric

B. not symmetric

Answer the questions below.

4. The data set at the right shows the hours that a group of students spent volunteering each weekend. Make a dot plot of the data. Then use your dot plot to complete Exercises 5-7.

Hours Spent Volunteering on Weekends 5, 3, 2, 6, 5, 4, 2, 14, 1, 2



5. Find the mean, median, and range of the data.

; median:_____; range:_____

6. Choose the best description of shape of the data distribution.

A. symmetric

B. not symmetric

7. 14 is far away from the other data. What is 14 called?



Reteach

Both stem-and-leaf plots and histograms can be used to display the same data. When intervals of 10 are used, you can compare the visual results.

Pounds of Newspapers Collected for Recycling						
12	28	24	32	35		
31	38	55	43	52		
42	49	18	22	15		
47	37	19	31	37		

Pounds of Newspapers

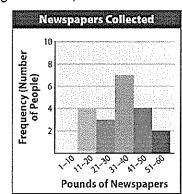
Interval	Frequency
1–10	0
11–20	4
21–30	3
31–40	7
41–50	4
51–60	2

In a **stem-and-leaf plot**, each data value consists of a stem and a leaf. In this case, the tens digit is the **stem** and the ones digit is the **leaf**.

Pounds of Newspapers Collected

Stem	Leaves
	2589
2	2 4 8
3	1125778
4	2379
5	2 5

A **histogram** is a bar graph in which the bars represent the frequencies of the numeric data within intervals. The bars on a histogram touch, but do not overlap.



Use the stem-and-leaf plot and histogram to complete Exercises 1-4.

- 1. How are the stem-and-leaf plot and histogram alike?
- 2. How do the stem-and-leaf plot and histogram differ?
- 3. Which display can you use to find the median?
- 4. What is the median of the data? _____
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Success for English Learners

Both the **stem-and-leaf plot** and the **histogram** provide a visual way to display data that involves greater numbers.

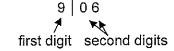
Problem 1

When you are looking for the individual values in a data set, you can use a stem-and-leaf plot.

stem-and-leaf plot

High	Temperatures
Stem	Leaves
6	058
7	25679
8	1
9	06
10	2

Reading the numbers:



So, 9 | 0 6 represents 90 and 96.

Problem 2

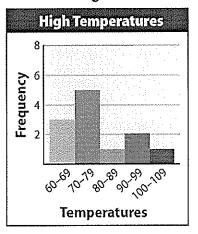
When you are not looking for the individual values in a data set, you can use a **frequency table** or a **histogram**.

frequency table

High Tem	peratures
Temperatures	Frequency
60–69	3
70–79	5
80–89	1
90–99	2
100–109	1
A	

The data is grouped by intervals instead of individual values.

histogram



- 1. Which display would you use if being able to identify the median and the mean is important? Explain.
- 2. What does the shape of the histogram tell you about the high temperatures?

17-4

Stem-and-Leaf Plots and Histograms

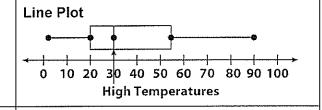
Reading Strategies: Compare and Contrast Displays

Statistical data can be displayed in different ways. Each of the following displays shows the high temperature on the 15th of each month in one city.

Ordered List

High Temperatures

2 15 18 22 30 30 30 32 45 65 65 90



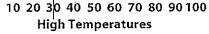
Frequency Table

High Temp	eratures
Temperatures	Frequency
0-19	3
20–39	5
40–59	1
60–79	2
80–99	1

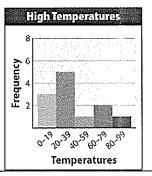
Stem-and-Leaf Plot

High	Temperatures
Stem	Leaves
0	2
1	5 8
2	2
3	0002
4	5
5	
6	5 5
7	
8	
9	0

Dot Plot



Histogram



1. Compare and contrast the ability to identify the measures of center with each type of display.



Practice and Problem Solving: A/B

Use the data at the right and the description below to complete Exercises 1–6.

The data set lists the heights of the Houston Rockets players during the 2011–2012 basketball season.

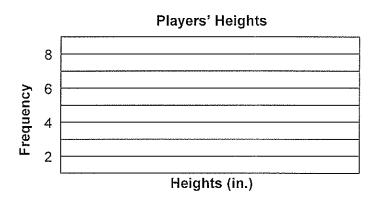
1. Complete the stem-and-leaf plot for the data.

Players' Heights					
Stem	Leaves				
6					
7					
8					

2. Complete the frequency table. Use an interval of 5.

Players'	Heights
Heights (in.)	Frequency
65–69	

3. Complete the histogram.



Players' Heights

72

87

71

81

80

80

80

80

79

79

76

81

72

65

77

79

82

82

Solve.

4. Find the range, the median, and the mean of the players' heights.

a. range

b. median

c. mode

Based on this data, what do you think is the average height of players in the National Basketball Association? Explain how you decided on your answer including which display of data you used.



Practice and Problem Solving: C

Use the data set at the right and the description below to complete Exercises 1-6.

The data set shows a list of the number of students at school each day during the month of January.

1. Complete the stem-and-leaf plot for the data.

Stud		:	0 -		_ 1
Stud	ents	ın	->-	:no	വ

Stem	Leaves
22	
23	
24	
25	
26	
27	
28	
29	

Students in School				
281	260	279	253	275
278	255	280	220	266
287	252	279	282	293
277	288	254	256	285

2. Complete the frequency table. 3. Complete the histogram. Use an interval of 20.

Students	in School
Number	Frequency
220–239	

Students in School

	8	
ncy	6	
Frequency	4	
ιĪ	2	

4. Find the range, the median, and the mean of the data.

Range: ______; Median: ______; Mean: _____

5. Identify the outlier and give a possible explanation for its occurrence.

6. Identify what effect, if any, the outlier has on the measures of center.

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Practice and Problem Solving: D

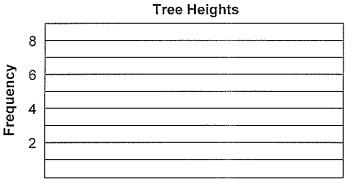
At the right is a list of the heights of trees that are for sale at a nursery. Use the data for Exercises 1–8. The first one is done for you.

Tree Heights								
70	75	65	70	74	64	77	61	
77	73	75	79	68	86	79	75	

Complete the frequency table.
 Use an interval of 5.

Tree He	ights
Heights (in.)	Frequency
60–64	2
65–69	2
70–74	4
75–79	7
80–84	0
85–89	1

2. Complete the histogram for the data.



3. Complete the stem-and-leaf plot for the data.

Tree Heights

٠	Stem	Leaves
•	6	
•	7	***************************************
•	8	

Answer the questions below. The first one is done for you.

- 4. What is the range of the tree heights? ______25
- 5. What is the median of the tree heights?
- 6. What is the mean of the tree heights? _____
- 7. The nursery wants a sign that tells what trees are available for sale by height. What measure of center would you use for the sign? _____
- 8. In the space below, make a sign for the trees for sale at the nursery.